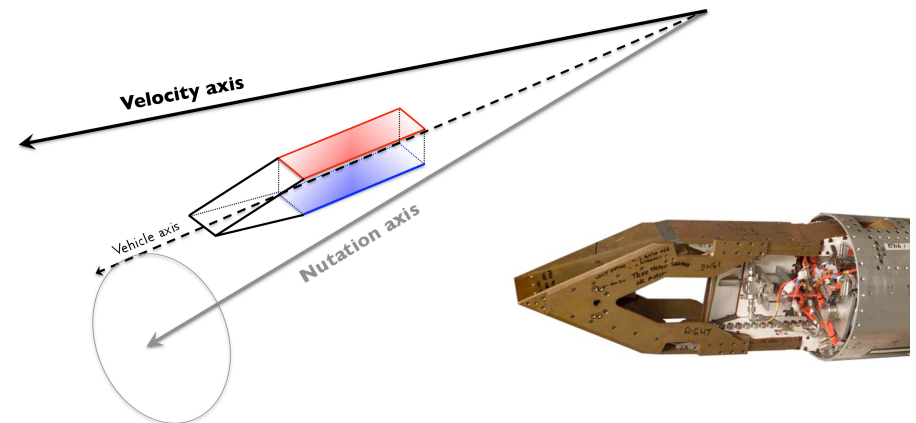
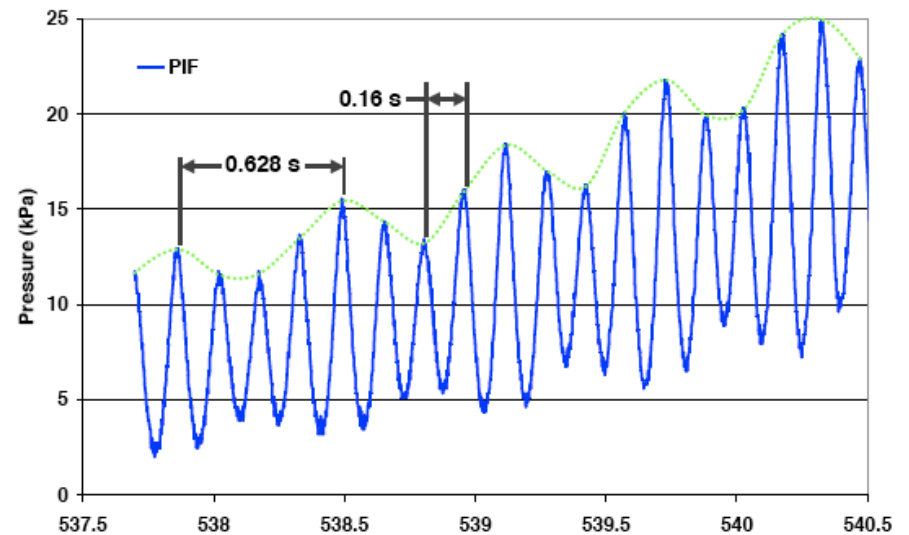
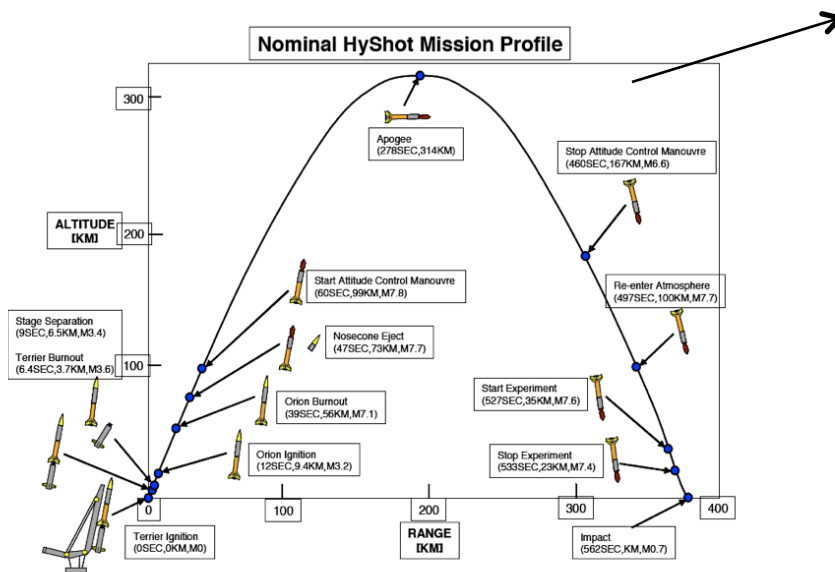


HyShot II – Flight Data Validation (revisited)

The flight conditions are **UNKNOWN**.

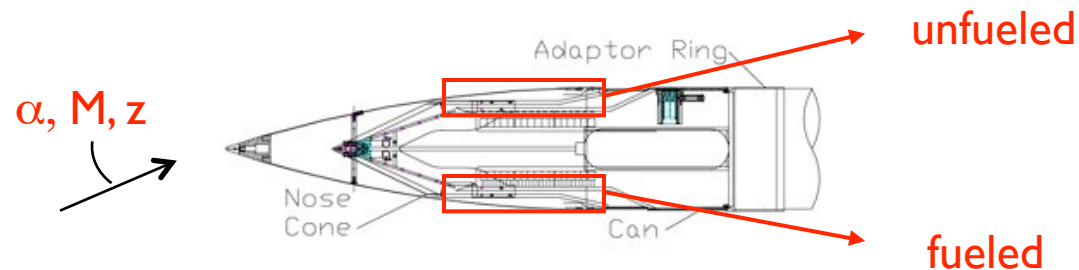
Extensive analysis by the Australian team attempted to back the flow conditions from a model of the trajectory!



HyShot II – Stochastic Inverse Problem

Our approach is based on inference; we solve a stochastic inverse problem (Bayesian)

Observation: two chambers are present (fueled and unfueled data)

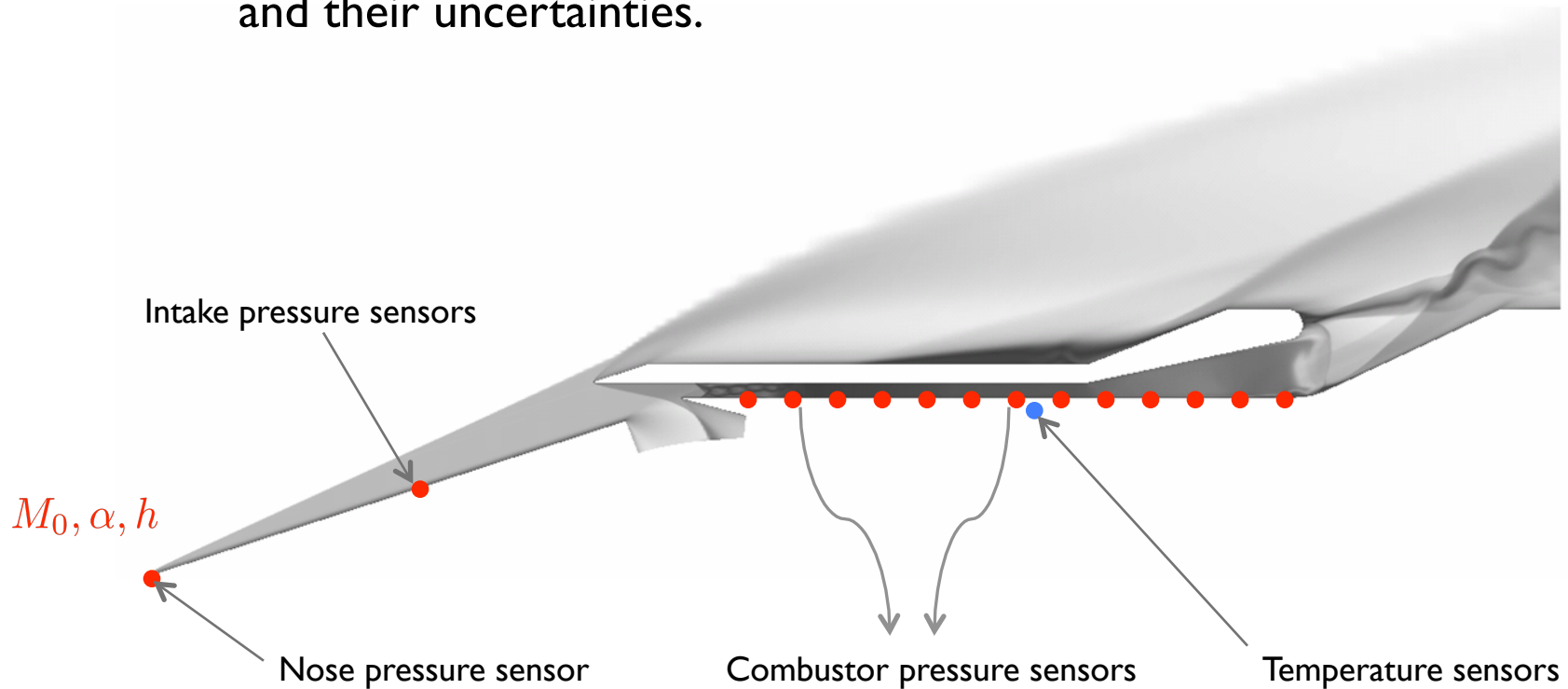
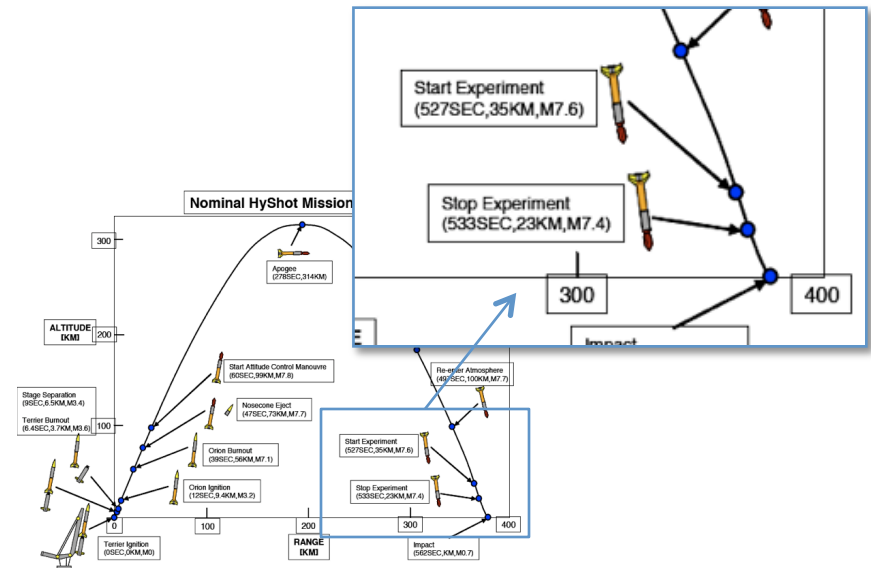


1. Build a forward model for the unfueled combustor
2. Use measurements to infer the flight data (conditioned by the forward model)
3. Predict the fueled side of the engine

HyShot II – Flight Data

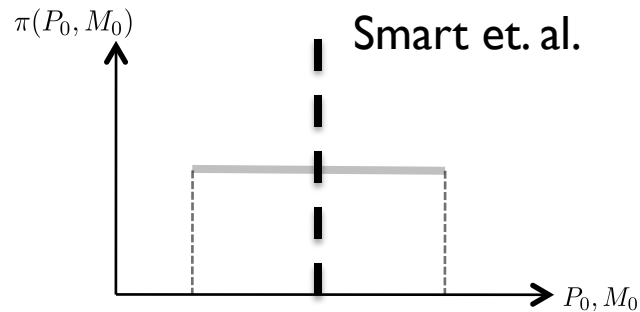
Given **noisy** measurements of pressure and temperature infer:

- Flight Mach number
- Angle of attack
- Vehicle altitude and their uncertainties.

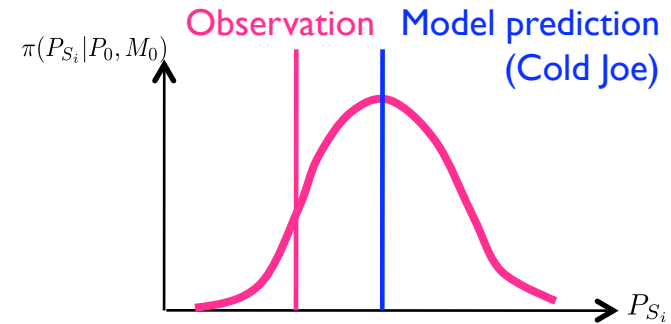


HyShot II – Bayesian Estimation

Prior distribution of parameters



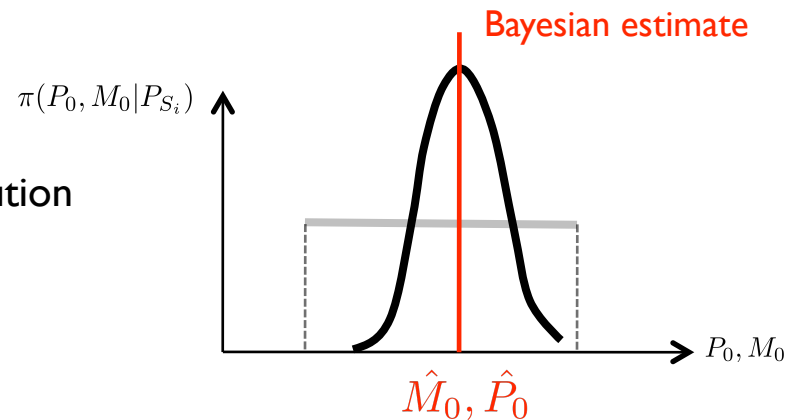
Measurement Uncertainties



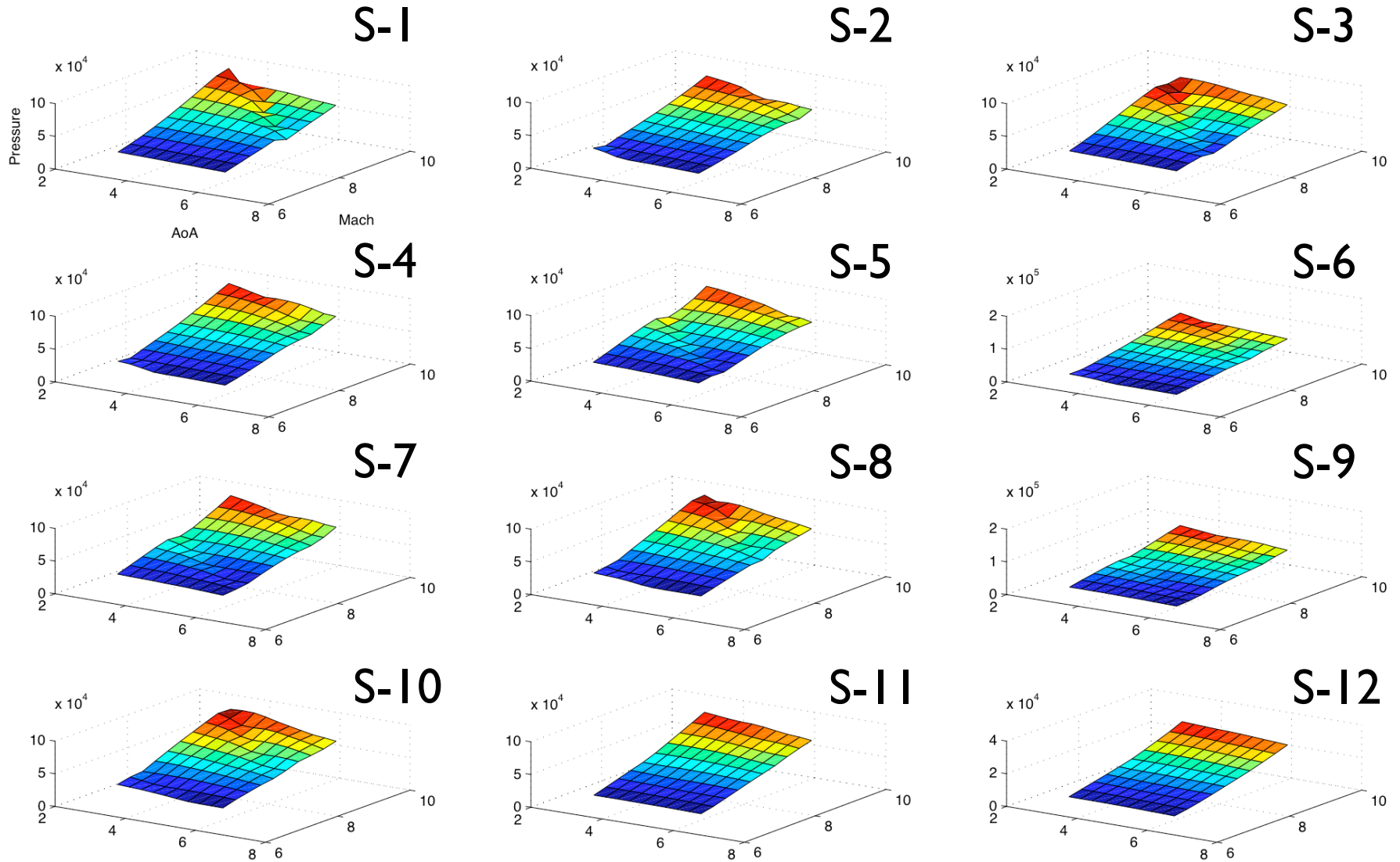
Bayes' Formula

$$\pi(P_0, M_0|P_{S_i}) \propto \pi(P_0, M_0) \cdot \pi(P_{S_i}|P_0, M_0)$$

Posterior distribution of parameters

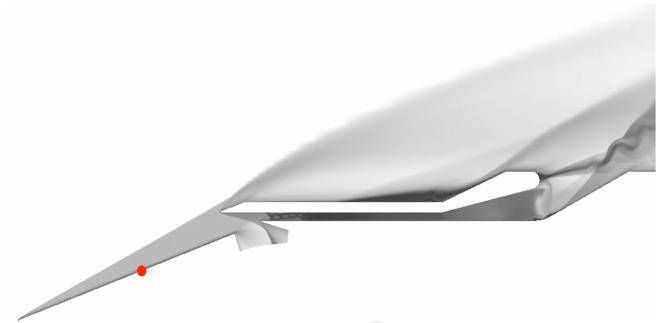


HyShot II – Forward Model

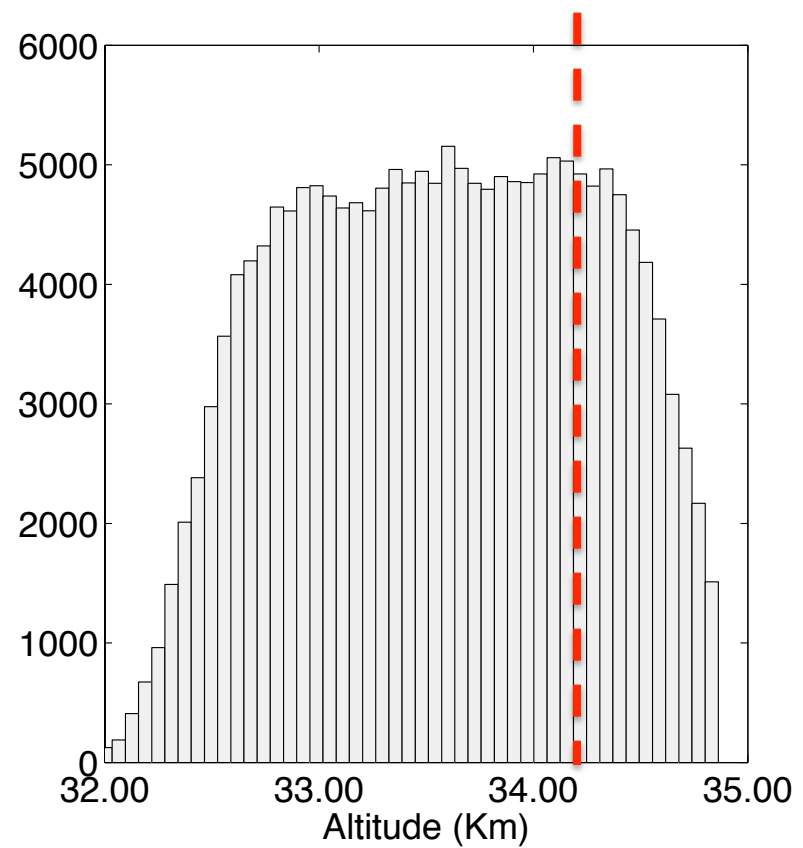
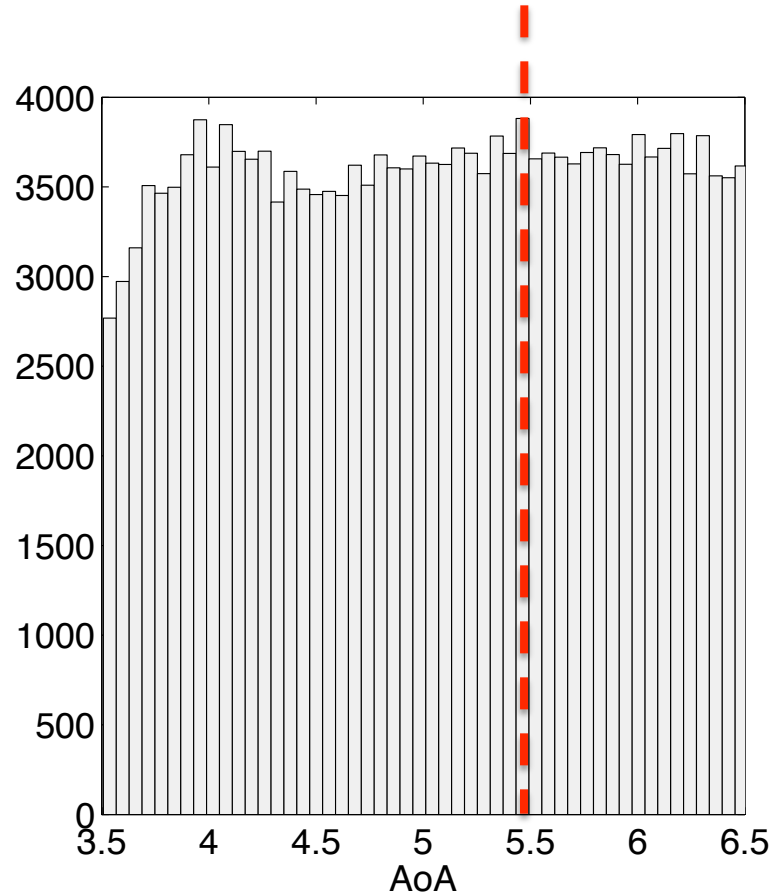


Computed pressure as function of flight Mach # and AoA (Fixed h=32km)

HyShot II – Inverse Analysis



Posterior Distributions

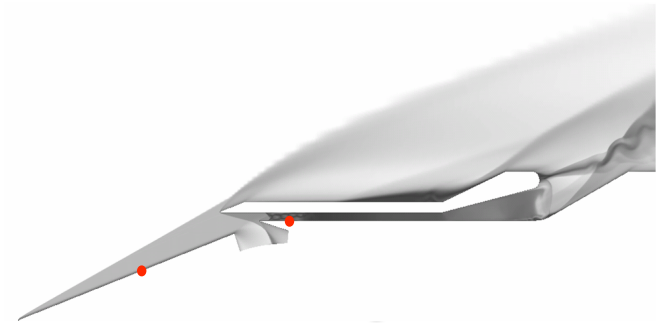
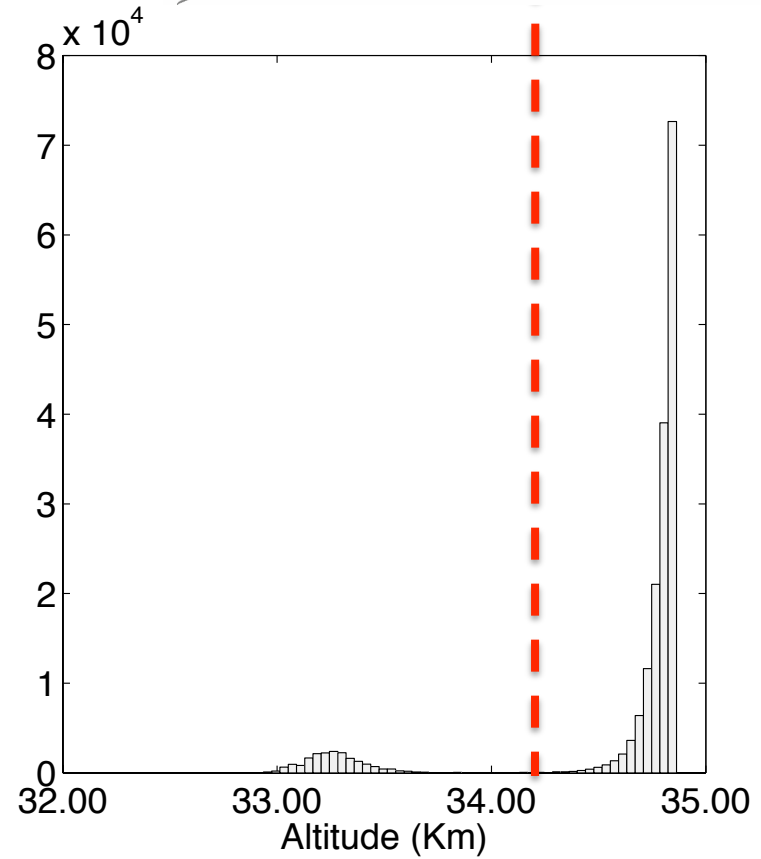
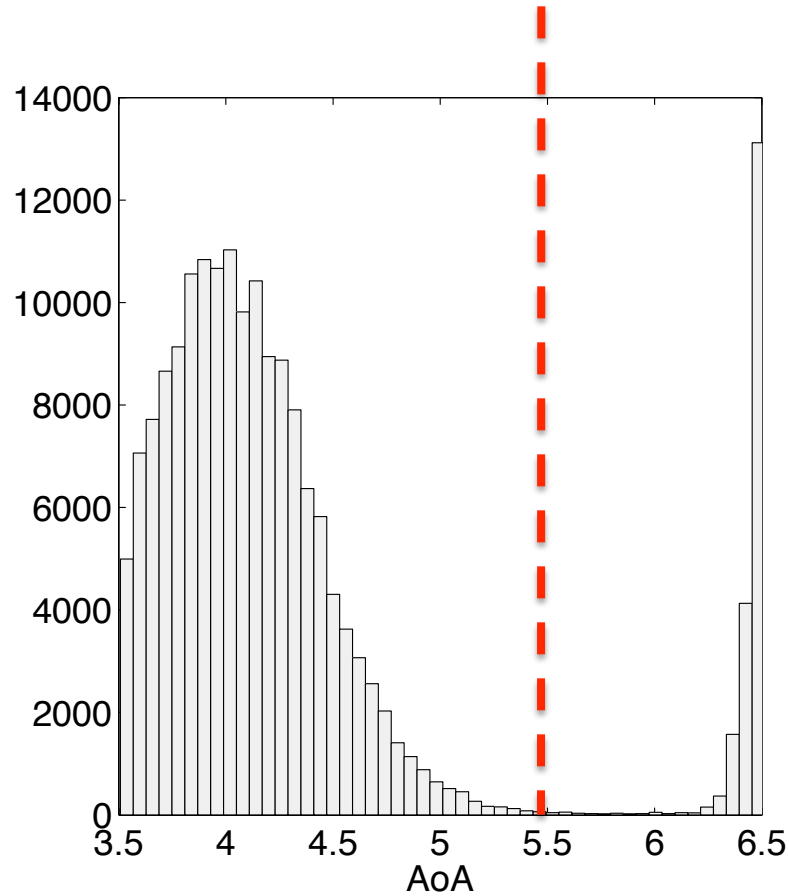


Intake Sensor

Smart et. al. - - -

HyShot II – Inverse Analysis

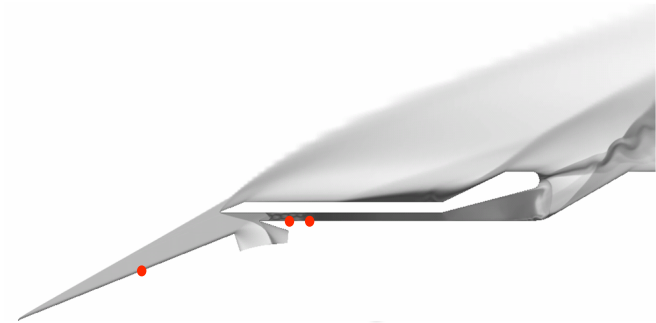
Posterior Distributions



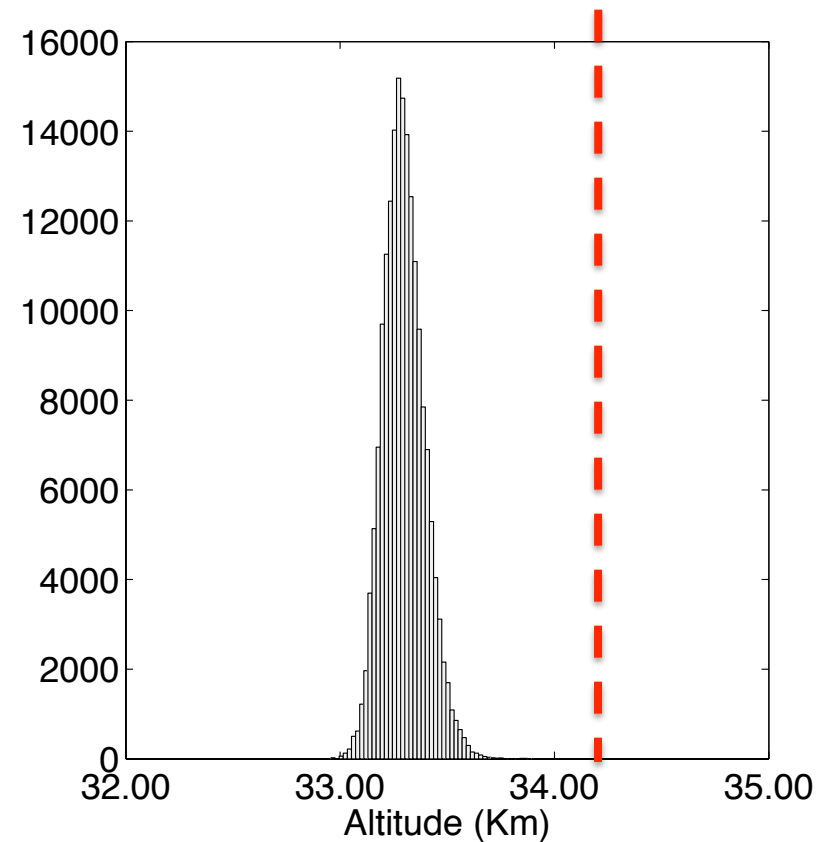
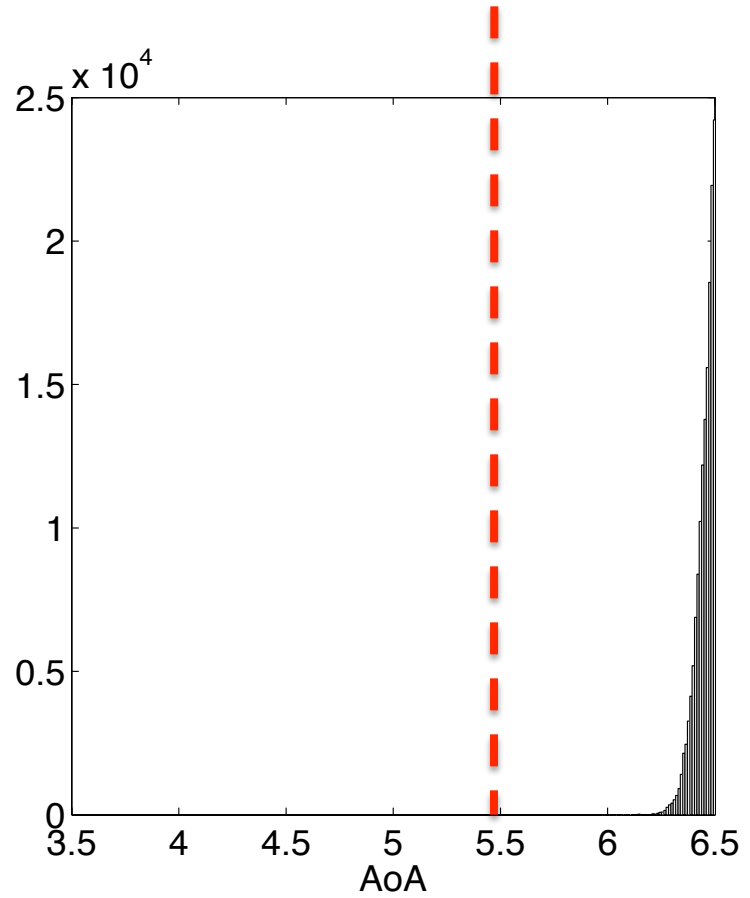
Intake Sensor + | Combustor Sensor

Smart et. al. - - -

HyShot II – Inverse Analysis



Posterior Distributions

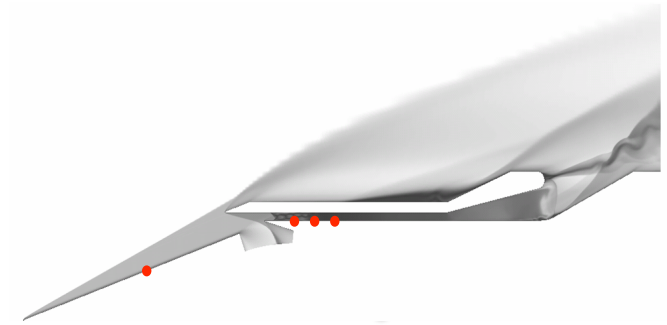
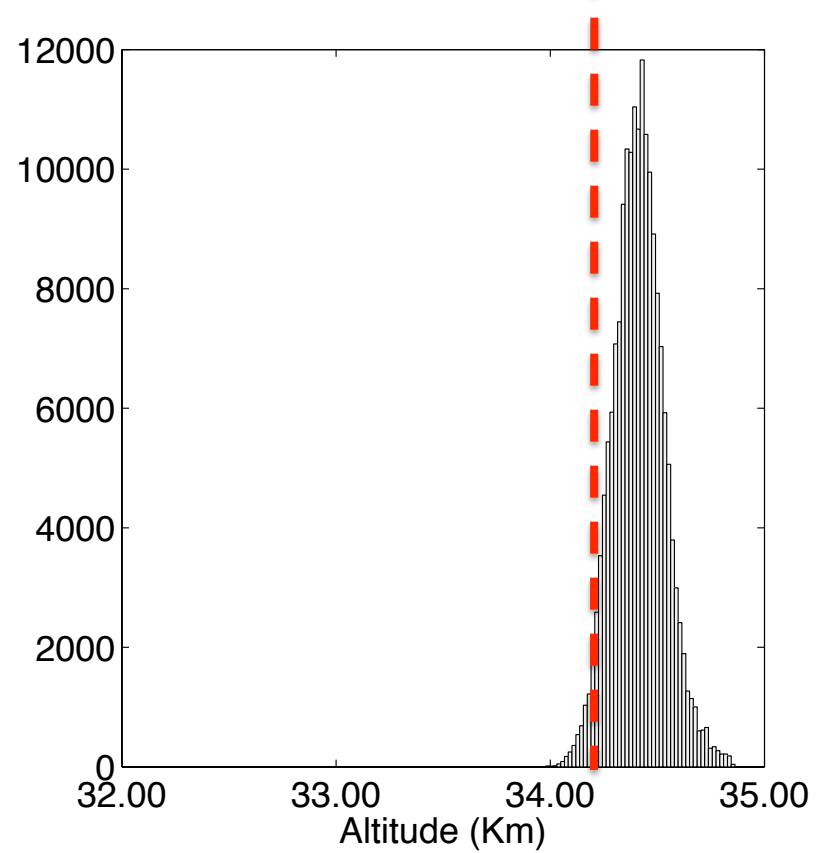
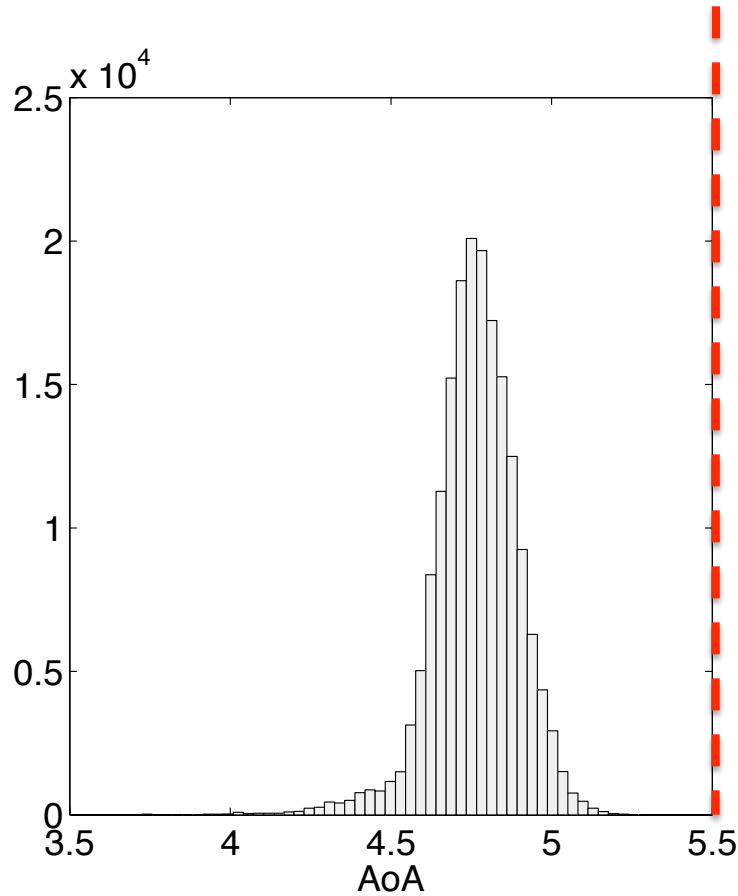


Intake Sensor + 2 Combustor Sensors

Smart et. al. - - -

HyShot II – Inverse Analysis

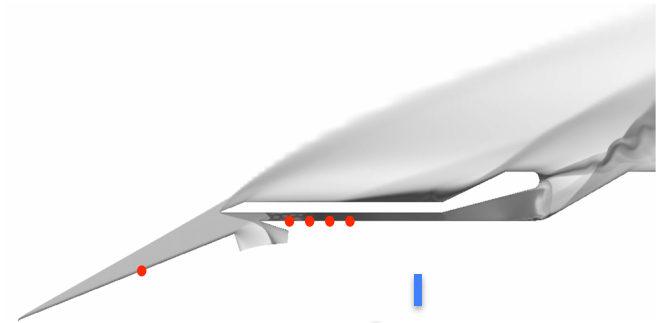
Posterior Distributions



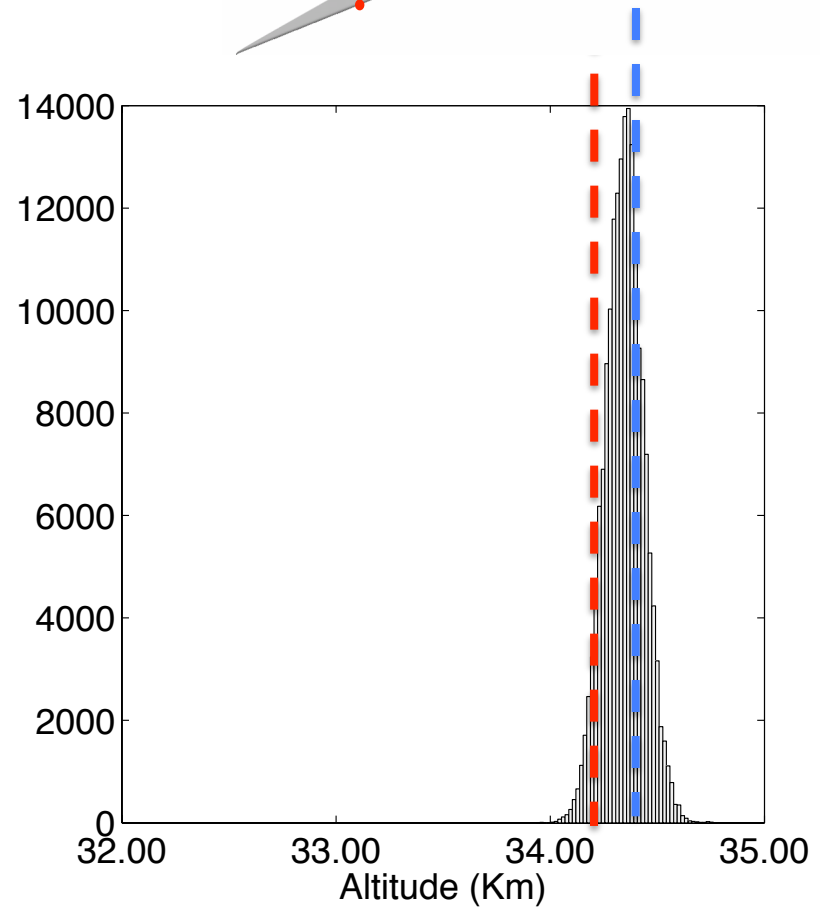
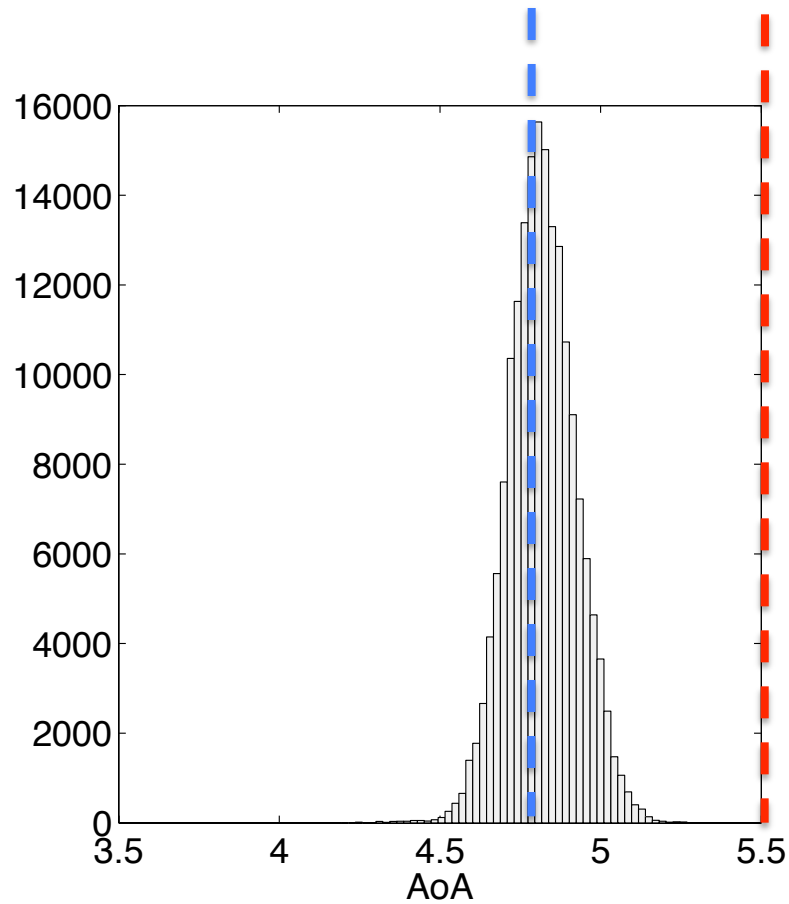
Intake Sensor + 3 Combustor Sensors

Smart et. al. - - -

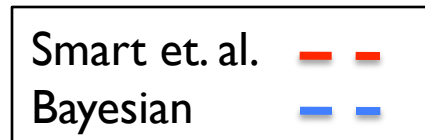
HyShot II – Inverse Analysis



Posterior Distributions

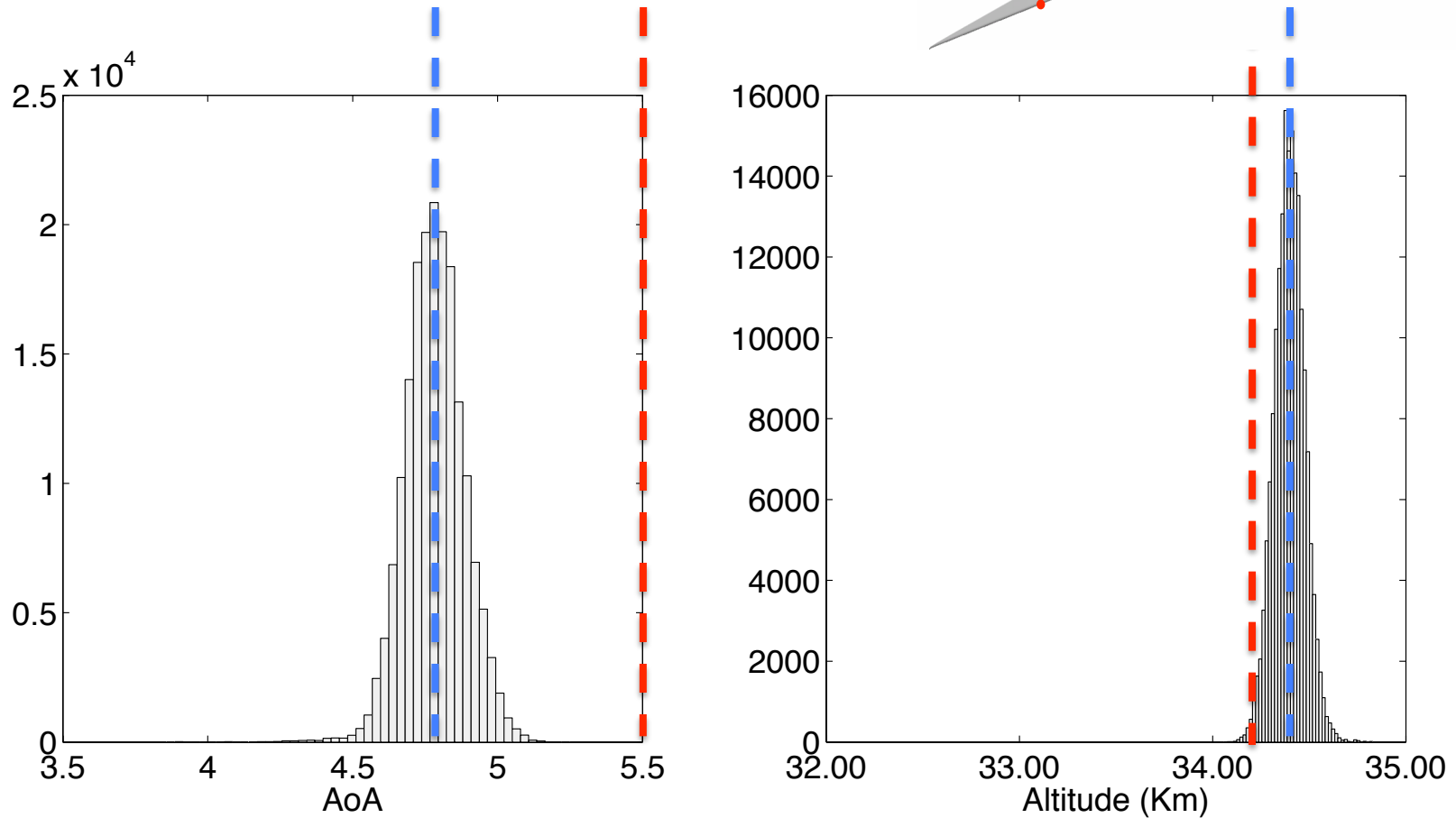


Intake Sensor + 4 Combustor Sensors

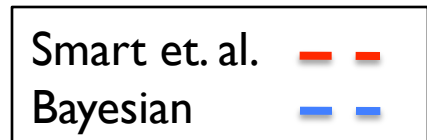


HyShot II – Inverse Analysis

Posterior Distributions

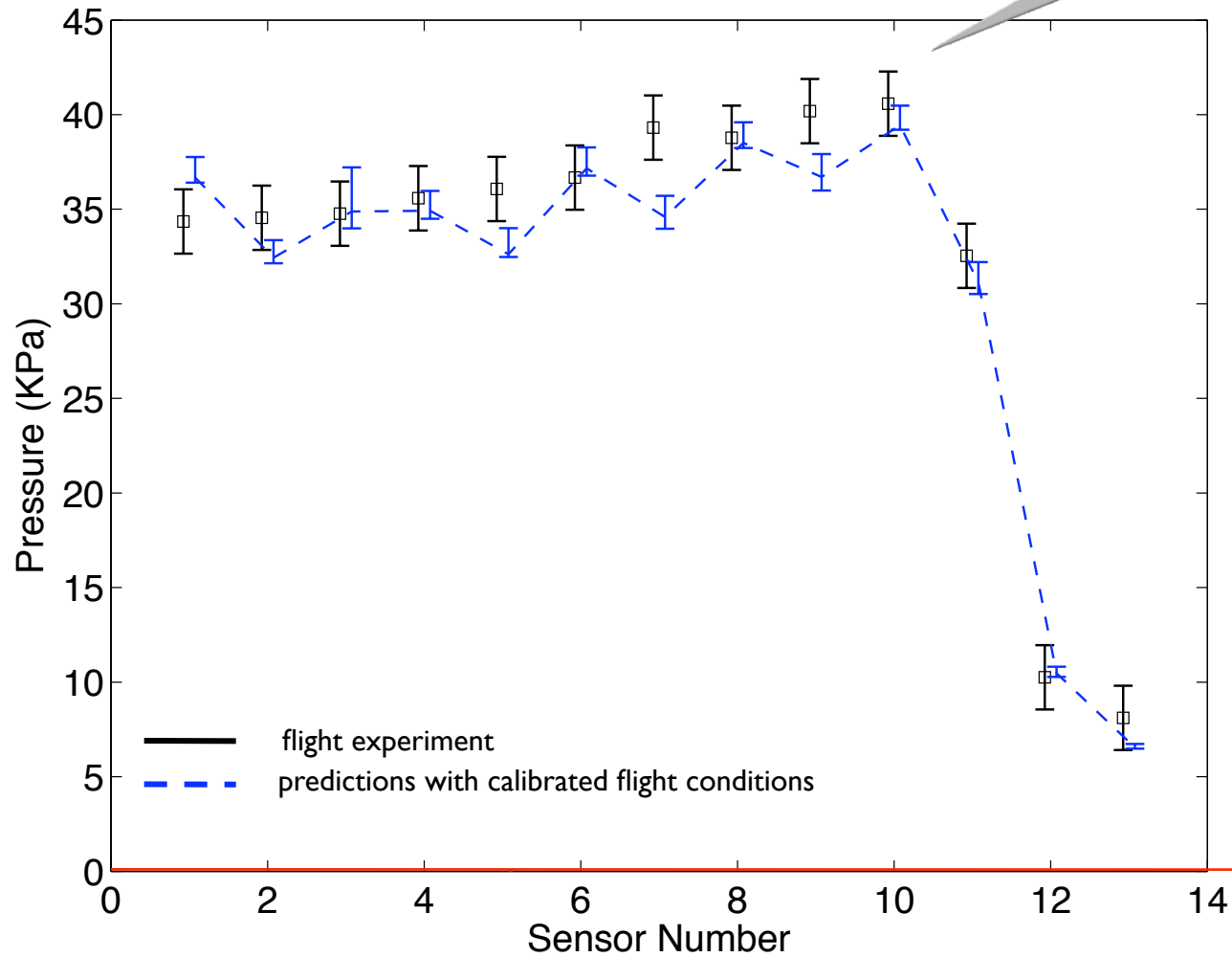


Intake Sensor + 5 Combustor Sensors



HyShot II – Inverse Analysis - Verification

A good match is expected by construction!



HyShot II – Inverse Analysis - Verification

